

B CONSTANTS & CONVERSION FACTORS

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UNIVERSAL CONSTANTS

[from US National Institute of Standards and Technology (NIST), based on 2014 CODATA]

- $c_0 = 299,792,458$ m/s = speed of light in a vacuum
 $c_1 = 3.741\ 771\ 790 \times 10^8$ W · m⁻² · μm⁴ = first radiation constant (in Planck's law)
 $c_{1B} = 1.191\ 042\ 953 \times 10^8$ W · m⁻² · μm⁴ · sr⁻¹ = first radiation constant for spectral radiance
 $c_2 = 1.438\ 777\ 36 \times 10^4$ μm · K = second radiation constant (in Planck's law)
 $G = 6.674\ 08 \times 10^{-11}$ m³ · s⁻² · kg⁻¹ = Newtonian gravitational constant
 $h = 6.626\ 070\ 040 \times 10^{-34}$ J · s = Planck constant
 $k_B = 1.380\ 648\ 52 \times 10^{-23}$ J · K⁻¹ · molecule⁻¹ = Boltzmann constant
 $N_A = 6.022\ 140\ 857 \times 10^{23}$ mol⁻¹ = Avogadro constant
 $\sigma_{SB} = 5.670\ 367 \times 10^{-8}$ W · m⁻² · K⁻⁴ = Stefan-Boltzmann constant
 $T = -273.15^\circ\text{C} = 0$ K = absolute zero (not considered a true universal constant)

MATH CONSTANTS

- [from *CRC Handbook of Chemistry and Physics*]
 $e = 2.718\ 281\ 828\ 459$ = base of natural logarithms
 $1/e = 0.367\ 879\ 441$ = e-folding ratio
 $\pi = 3.141\ 592\ 653\ 589\ 793\ 238\ 462\ 643$ = pi
 $\text{sqrt}(2) = 1.414\ 213\ 562\ 373\ 095$



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EARTH CHARACTERISTICS

- 1° latitude = 111 km = 60 nautical miles (nm) [Caution: This relationship does NOT hold for degrees longitude.]
 $a = 149.598$ Gm = semi-major axis of Earth orbit
 $A = 0.306$ = Bond albedo (NASA 2015)
 $A = 0.367$ = visual geometric albedo (NASA 2015)
 $b = 149.090$ Gm = semi-minor axis of Earth orbit
 $d = 149.597\ 870\ 7$ Gm = average sun-Earth distance = 1 Astronomical Unit (AU) (NASA 2015)
 $d_{\text{aphelion}} = 152.10$ Gm = furthest sun-Earth distance, which occurs about 4 July (NASA 2015)
 $d_{\text{perihelion}} = 147.09$ Gm = closest sun-Earth distance, which occurs about 3 January (NASA 2015)
 $d_r = 173 = 22$ June = approx. day of summer solstice
 $e = 0.0167$ = eccentricity of Earth orbit around sun
 $g = -9.806\ 65$ m · s⁻² = average gravitational acceleration on Earth at sea level (negative = downward). (from 2014 CODATA)
 $|g| = g_0 \cdot [1 + A \cdot \sin^2(\phi) - B \cdot \sin^2(2\phi)] - C \cdot H$
 = variation of gravitational-acceleration magnitude with latitude ϕ and altitude H (m) above mean sea level. $g_0 = 9.780\ 318\ 4$ m · s⁻², $A = 0.005\ 3024$, $B = 0.000\ 0059$, $C = 3.086 \times 10^{-6}$ s⁻².
 $M = 5.9726 \times 10^{24}$ kg = mass of Earth (NASA 2015)
 $P_{\text{earth}} = 365.256$ days = Earth orbital period (2015)
 $P_{\text{moon}} = 27.3217$ days = lunar orbital period (2015)
 $P_{\text{sidereal}} = 23.934\ 469\ 6$ h = sidereal day = period for one revolution of the Earth about its axis, relative to fixed stars
 $R_{\text{earth}} = 6371.0$ km = volumetric average Earth radius (from NASA 2015)
 = 6378.1 km = Earth radius at equator
 = 6356.8 km = Earth radius at poles
 $S = 1367.6$ W · m⁻² = solar irradiance (solar constant) at top of atmosphere (NASA 2015)
 ≈ 1.125 K · m · s⁻¹ = kinematic solar constant (based on mean sea-level density)
 $T_e = 254.3$ K = effective radiation emission black-body temperature of Earth system (NASA 2015)
 $\Phi_r = 23.44^\circ = 0.4091$ radians = tilt of Earth axis = obliquity relative to the orbital plane (2015)
 $\Omega = 0.729\ 210\ 7 \times 10^{-4}$ s⁻¹ = sidereal rotation frequency of Earth (NASA 2015)
 $2\Omega = 1.458\ 421 \times 10^{-4}$ s⁻¹ = Coriolis factor
 $2\Omega / R_{\text{earth}} = 2.289 \times 10^{-11}$ m⁻¹ · s⁻¹ = beta factor

AIR AND WATER CHARACTERISTICS

$a = 0.0337 \text{ (mm/day)} \cdot (\text{W/m}^2)^{-1}$ = water depth evaporation per latent heat flux
 $B = 3 \times 10^9 \text{ V/km}$ = breakdown potential for dry air
 $C_{vd} = 717 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for dry air at constant volume
 $C_{pd} = 1003 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for dry air at constant pressure at -23°C
 $C_{pd} = 1004 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for dry air at constant pressure at 0°C
 $C_{pd} = 1005 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for dry air at constant pressure at 27°C
 $C_{pv} = 1850 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for water vapor at constant pressure at 0°C
 $C_{pv} = 1875 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat for water vapor at constant pressure at 15°C
 $C_{liq} = 4217.6 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat of liquid water at 0°C
 $C_{ice} = 2106 \text{ J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ = specific heat of ice at 0°C
 $D = 2.11 \times 10^{-5} \text{ m}^2 \cdot \text{s}^{-1}$ = molecular diffusivity of water vapor in air in standard conditions
 $e_o = 0.611 \text{ kPa}$ = reference vapor pressure at 0°C
 $k = 0.0253 \text{ W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ = molecular conductivity of air at sea level in standard conditions
 $L_d = 2.834 \times 10^6 \text{ J} \cdot \text{kg}^{-1}$ = latent heat of deposition at 0°C
 $L_f = 3.34 \times 10^5 \text{ J} \cdot \text{kg}^{-1}$ = latent heat of fusion at 0°C
 $L_v = 2.501 \times 10^6 \text{ J} \cdot \text{kg}^{-1}$ = latent heat of vaporization at 0°C
 $n = 3.3 \times 10^{28} \text{ molecules} \cdot \text{m}^{-3}$ for liquid water at 0°C
 $n_{air} \approx 1.000277$ = index of refraction for air
 $n_{water} \approx 1.336$ = index of refraction for liquid water
 $n_{ice} \approx 1.312$ = index of refraction for ice
 $P_{STP} = 101.325 \text{ kPa}$ = standard sea-level pressure (STP = Standard Temperature & Pressure)
 $\mathfrak{R}_d = 0.287053 \text{ kPa} \cdot \text{K}^{-1} \cdot \text{m}^3 \cdot \text{kg}^{-1} = C_{pd} - C_{vd}$
 $= 287.053 \text{ J} \cdot \text{K}^{-1} \cdot \text{kg}^{-1}$ = gas constant for dry air
 $\mathfrak{R}_v = 461.5 \text{ J} \cdot \text{K}^{-1} \cdot \text{kg}^{-1}$ = water-vapor gas constant
 $= 4.61 \times 10^{-4} \text{ kPa} \cdot \text{K}^{-1} \cdot \text{m}^3 \cdot \text{g}^{-1}$
 $Ri_c = 0.25$ = critical Richardson number
 $s_o = 343.15 \text{ m/s}$ = sound speed in standard, calm air
 $T_{STP} = 15^\circ\text{C}$ = standard sea-level temperature
 $\varepsilon = 0.622 \text{ g}_{\text{water}} \cdot \text{g}_{\text{air}}^{-1} = \mathfrak{R}_d / \mathfrak{R}_v$ = gas-constant ratio
 $\gamma = 0.0004 \text{ (g}_{\text{water}} \cdot \text{g}_{\text{air}}^{-1}) \cdot \text{K}^{-1} = C_p / L_v$
 $= 0.4 \text{ (g}_{\text{water}} \cdot \text{kg}_{\text{air}}^{-1}) \cdot \text{K}^{-1}$ = psychrometric constant
 $\Gamma_d = 9.75 \text{ K} \cdot \text{km}^{-1} = |g| / C_p$ = dry adiabatic lapse rate
 $\rho_{STP} = 1.225 \text{ kg} \cdot \text{m}^{-3}$ = standard sea-level air density
 $\rho_{avg} = 0.689 \text{ kg} \cdot \text{m}^{-3}$ = air density averaged over the troposphere (over $z = 0$ to 11 km)

$\rho_{liq} = 999.84 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 0°C
 $= 1000.0 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 4°C
 $= 998.21 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 20°C
 $= 992.22 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 40°C
 $= 983.20 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 60°C
 $= 971.82 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 80°C
 $= 958.40 \text{ kg} \cdot \text{m}^{-3}$ = density of liquid water at 100°C
 $\rho_{sea-water} = 1025 \text{ kg} \cdot \text{m}^{-3}$ = avg. density of sea water, (sea water contains 34.482 g of salt ions per kg of water, on average)
 $\rho_{ice} = 916.8 \text{ kg} \cdot \text{m}^{-3}$ = density of ice at 0°C
 $\sigma = 0.076 \text{ N} \cdot \text{m}^{-1}$ = surface tension of pure water 0°C

CONVERSION FACTORS & COMBINED PARAMETERS

$C_{pd} / C_{vd} = k = 1.400$ (dimensionless)
 $=$ specific heat ratio
 $C_{pd} / |g| = 102.52 \text{ m} \cdot \text{K}^{-1}$
 $C_{pd} / L_v = 0.0004 \text{ (g}_{\text{water}} \cdot \text{g}_{\text{air}}^{-1}) \cdot \text{K}^{-1} = \gamma$
 $= 0.4 \text{ (g}_{\text{water}} \cdot \text{kg}_{\text{air}}^{-1}) \cdot \text{K}^{-1}$
 $=$ psychrometric constant
 $C_{pd} / \mathfrak{R}_d = 3.50$ (dimensionless)
 $C_{vd} / C_{pd} = 1/k = 0.714$ (dimensionless)
 $|g| / C_{pd} = \Gamma_d = 9.8 \text{ K} \cdot \text{km}^{-1}$ = dry adiabatic lapse rate
 $|g| / \mathfrak{R}_d = 0.0342 \text{ K} \cdot \text{m}^{-1} = 1/(\text{hypsometric constant})$
 $L_v / C_{pd} = 2.5 \text{ K} / (\text{g}_{\text{water}} \cdot \text{kg}_{\text{air}}^{-1})$
 $L_v / \mathfrak{R}_v = 5423 \text{ K} =$ Clausius-Clapeyron parameter for vaporization
 $\mathfrak{R}_d / C_{pd} = 0.28571$ (dimensionless) = potential-temperature constant
 $\mathfrak{R}_d / \mathfrak{R}_v = \varepsilon = 0.622 \text{ g}_{\text{water}} \cdot \text{g}_{\text{air}}^{-1} =$ gas-constant ratio
 $\mathfrak{R}_d / |g| = 29.29 \text{ m} \cdot \text{K}^{-1} =$ hypsometric constant
 $\rho_{air} \cdot C_{pd,air} = 1231 \text{ (W} \cdot \text{m}^{-2}) / (\text{K} \cdot \text{m} \cdot \text{s}^{-1})$ at sea level
 $= 12.31 \text{ mb} \cdot \text{K}^{-1}$ at sea level
 $= 1.231 \text{ kPa} \cdot \text{K}^{-1}$ at sea level
 $\rho_{air} \cdot |g| = 12.0 \text{ kg} \cdot \text{m}^{-2} \cdot \text{s}^{-2}$ at sea level
 $= 0.12 \text{ mb} \cdot \text{m}^{-1}$ at sea level
 $= 0.012 \text{ kPa} \cdot \text{m}^{-1}$ at sea level
 $\rho_{air} \cdot L_v = 3013.5 \text{ (W} \cdot \text{m}^{-2}) / [(\text{g}_{\text{water}} \cdot \text{kg}_{\text{air}}^{-1}) \cdot (\text{m} \cdot \text{s}^{-1})]$ at sea level
 $\rho_{liq} \cdot C_{liq} = 4.295 \times 10^6 \text{ (W} \cdot \text{m}^{-2}) / (\text{K} \cdot \text{m} \cdot \text{s}^{-1})$
 $1 \text{ megaton nuclear explosion} \approx 4 \times 10^{15} \text{ J}$
 $2\pi \text{ radians} = 360^\circ$
 $(1-\varepsilon)/\varepsilon = 0.61 =$ virtual temperature constant